

## Another Domino Dilemma

Did you know that the white spots on dominos are called pips?  
Figure out the number of pips in a box of dominos without using any dominos.

**Grade Levels 3 - 5**

## **Another Domino Dilemma**

Did you know that the white spots on dominos are called pips? Figure out the number of pips in a box of dominos without using any dominos.

### **Context**

Two months ago we had given this class of fourth and fifth grade students several domino tasks from which they could choose which ones they wanted to solve. Well, here is another! It was helpful for students to have solved the other "Domino Dilemma" before completing this one (Miss Amico's crazy Italian grandparents have a set of dominos with the digits 0 - 9 on them. Dominos we commonly use have digits 0 - 6 on them and come 28 in a set. How many dominos come in a set with digits 0 - 9 on them?)

### **What This Task Accomplishes**

This task assesses student's ability to find a pattern (in order to figure out all possible domino pip combinations) and then to create an organized method for determining the sum of the pips.

### **What the Student Will Do**

Most students will create a list of all possible domino combinations, usually in some organized fashion and then will do some subtotaling and then find the grand total of their results.

### **Time Required for Task**

60 minutes

### **Interdisciplinary Links**

The studies of games and other forms of entertainment.

### **Teaching Tips**

Make sure students have lots of opportunities to work with dominos before giving this task. Also, we adapted the task for a student in the class who has special needs and who had an IEP goal of understanding "more than" and "less than".

Which dominos have more than 8 pips? Which dominos have less than 8 pips?

### **Suggested Materials**

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# Exemplars

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- Dominos
- Calculators
- Graph paper

## Possible Solutions

There are 168 pips.

## Benchmark Descriptors

### Novice

Although this student finds the correct solution, his/her process of finding the total is awkward and rudimentary. His/her work lacks organization and is difficult to follow. S/he uses math language incorrectly and his/her representation lacks labels.

### Apprentice

This student arrives at an incorrect answer, which if s/he had gone back and checked his/her work could have been remedied. S/he has an interesting way of finding all domino combinations, which could have been more clearly presented. The reader has to fill in many details to understand what was done. This student's work has good potential and s/he should be encouraged to go back and make revisions to better communicate his/her solution.

### Practitioner

This student uses a systematic approach to solving the task by finding a pattern and creates a representation to express his/her solution. This student could be encouraged to look more closely at his/her results to see if s/he can notice any patterns, relationships or generalizations and probably could do so given the organization s/he used in his/her approach. His/her representation could be labeled and his/her communication more clear.

### Expert

This student solves the task in a similar way to his/her peers, but creates a novel way of finding the total. S/he then solves the problem again, using the same strategy, for dominos having 0 - 9 pips. It would have been neat if the student had been able to verify his/her solution to the task using his/her extension as a way of verifying his/her solution.

# Exemplars

## Novice

The student incorrectly uses the terms "average" and "graph".

Dear Mrs. Amico,  
the math problem I just did  
was Domino dilemma #4. In this  
problem they asked me to find  
out the number of pips in a  
set of dominoes.

I figured out this problem  
by making a stair case shaped  
graph. then I started to add  
all of the numbers up until  
I came up to an average  
of one hundred and sixty eight.  
That's how I figured it  
out.

# Exemplars

## Novice

6							
6							
5	5						
5	6						
4	4	4					
4	5	6					
3	3	3	3				
3	4	5	6				
2	2	2	2	2			
2	3	4	5	6			
1	1	1	1	1	1		
1	1	3	4	5	6		
0	0	0	0	0	0	0	
0	1	2	3	4	5	6	

# Exemplars

## Novice

$$\begin{array}{r} 6 \\ + 6 \\ \hline 12 \end{array}$$

$$\begin{array}{r} 12 \\ + 10 \\ \hline 22 \end{array}$$

$$\begin{array}{r} 22 \\ + 11 \\ \hline 33 \end{array}$$

$$\begin{array}{r} 33 \\ + 8 \\ \hline 41 \end{array}$$

$$\begin{array}{r} 41 \\ + 9 \\ \hline 50 \end{array}$$

$$\begin{array}{r} 50 \\ + 10 \\ \hline 60 \end{array}$$

$$\begin{array}{r} 60 \\ + 6 \\ \hline 66 \end{array}$$

$$\begin{array}{r} 66 \\ + 7 \\ \hline 73 \end{array}$$

$$\begin{array}{r} 73 \\ + 8 \\ \hline 81 \end{array}$$

$$\begin{array}{r} 81 \\ + 9 \\ \hline 90 \end{array}$$

$$\begin{array}{r} 90 \\ + 4 \\ \hline 94 \end{array}$$

$$\begin{array}{r} 94 \\ + 5 \\ \hline 99 \end{array}$$

$$\begin{array}{r} 99 \\ + 6 \\ \hline 105 \end{array}$$

$$\begin{array}{r} 7 \\ \hline 112 \end{array}$$

$$\begin{array}{r} 112 \\ + 8 \\ \hline 120 \end{array}$$

$$\begin{array}{r} 120 \\ + 2 \\ \hline 122 \end{array}$$

$$\begin{array}{r} 122 \\ + 3 \\ \hline 125 \end{array}$$

$$\begin{array}{r} 125 \\ + 4 \\ \hline 129 \end{array}$$

$$\begin{array}{r} 129 \\ + 5 \\ \hline 134 \end{array}$$

$$\begin{array}{r} 134 \\ + 6 \\ \hline 140 \end{array}$$

$$\begin{array}{r} 140 \\ + 7 \\ \hline 147 \end{array}$$

$$\begin{array}{r} 147 \\ + 1 \\ \hline 148 \end{array}$$

$$\begin{array}{r} 148 \\ + 2 \\ \hline 150 \end{array}$$

$$\begin{array}{r} 150 \\ + 3 \\ \hline 154 \end{array}$$

$$\begin{array}{r} 153 \\ + 4 \\ \hline 157 \end{array}$$

$$\begin{array}{r} 157 \\ + 5 \\ \hline 162 \end{array}$$

$$\begin{array}{r} 162 \\ + 6 \\ \hline 168 \end{array}$$


This student uses a very awkward means of finding the sum, but does obtain a correct solution. The work is not organized and is difficult to follow.

# Exemplars

## Apprentice

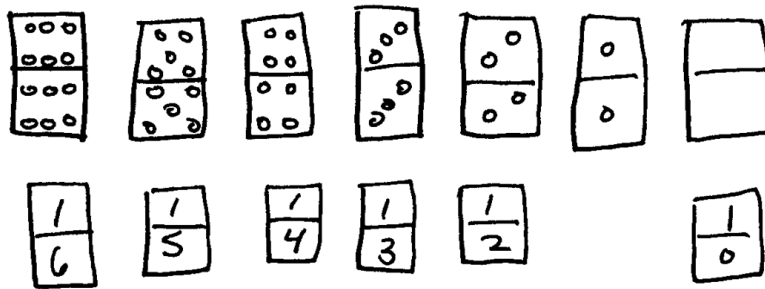
This student clearly communicates her/his strategy, but in some places (especially on the next page) the reader has to fill in details for the solution to make sense.

Dear Miss Amico

I did Domino Dilemma #4. I found there are 165 pips in a regular set of 28 dominos. Let me explain further. I drew all the doubles, (have the (same number of Pips. on top as on the bottom.) then, like under , I would draw 6 pips over 5 pips, 6 pips over 4 pips, and so on. I did that with all other doubles. Then I wrote the number of Pips on each double and added them up. 42 I did that with all the dominos with one pip on top and 1-6 on the bottom. I did that with dominos with 2 Pips on top, 3, 4, 5 and 6. I added all the sums together, and got 165.

# Exemplars

## Apprentice



Here the student misses 2/0.

12 Pips	7	8	9	10
10 Pips	6	7	8	9
8 Pips	5	6	7	4
6 Pips	4	5	5	23
4 Pips	3	26	27	
+ 2 Pips				5
	42	25		6
				22

$\frac{2}{6}$	$\frac{2}{5}$	$\frac{2}{4}$	$\frac{2}{3}$	$\frac{2}{2}$
---------------	---------------	---------------	---------------	---------------

Here the student makes a computation mistake.

$\frac{3}{6}$	$\frac{3}{5}$	$\frac{3}{4}$	$\frac{3}{0}$
---------------	---------------	---------------	---------------

$\frac{4}{6}$	$\frac{4}{5}$	$\frac{4}{0}$
---------------	---------------	---------------

$\frac{5}{6}$	$\frac{5}{0}$
---------------	---------------

This student attempts to use an organized system for solving the task, which is complicated, but would have worked if the student had gone back and checked his/her work.

42
25
26
27
23
23
<u>165</u>

## Another Domino Dilemma



# Exemplars

## Practitioner

### 1-Centimeter Squares

0	0	0	0	0	0	0
0	1	2	3	4	5	6
1	1	1	1	1	1	
1	2	3	4	5	6	

This student arrives a correct solution but could communicate more clearly how s/he solved the task.

2	2	2	2	2
2	3	4	5	6

This student's work, although brief, is well organized and accurate.

3	3	3	3
3	4	5	6

4	4	4
4	5	6

Here it would have been great if the student noticed that each column sum decreases by a multiple of 6!

5	5
5	6

6

6

168

42 36 30 24 18 12 6 = 168 pips in a box

# Exemplars

## Practitioner

0 0 0 0 0 0 0  
0 1 2 3 4 5 6

1 1 1 1 1 1  
1 2 3 4 5 6

2 2 2 2 2  
2 3 4 5 6

3 3 3 3  
3 4 5 6

4 4 4  
4 5 6

5 5  
5 6

6  
6

and  
168

was my answer

and that  
is how I  
did it and  
then I went  
like this  
↓

42 36 30 24  
1812 6 = 168  
pips in a Box

168!

# Exemplars

## Expert

Dear Mrs. McKeqney

The student explains how she/he solves the problem.

First I made a set of dominoes on a piece of graph paper. then I kept adding the pips on the dominoes together until I got the answer the next thing I did is labeled it, the total number of pips in a box is 168

# Exemplars

## Expert

Set of Dominoes								the									
								S									
								U									
								M									
6								6									
6								6	12								
5	5							10									
5	6							11	21								
4	4	4						12	21	48	60						
4	5	6						15									
3	3	3	3					12									
3	4	5	6					18	30			168					
2	2	2	2	2				10									
2	3	4	5	6				20	30	60	108						
1	1	1	1	1	1			6									
1	2	3	4	5	6			21	27	48							
0	1	2	5	4	5	6		21	21								
0	0	0	0	0	0	0	0	0	21								

total answer of pips  
in a box.

total answer of Pips  
in a box.

The student's strategy of creating an organized list and creating a flow chart for finding the sum would work for this problem.

The student's work is labeled and accurate.

