Telephone Numbers

A telephone number has 3 parts: an area code, an exchange and a suffix.

How many different telephone numbers are possible? Are all of these probable?

Exemplars

Grade Levels 6 - 8

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Context

We had worked with exponents and combination problems. I wanted a problem that would combine the two concepts.

What This Task Accomplishes

This is a real-world application. I was looking to see who could come up with the idea of combinations, but also to see who would take this task realistically. Some research would be necessary for a deep understanding of the problem.

What the Student Will Do

Many students began with 10 possibilities for each slot in the telephone number. Many used exponents successfully. There were many different levels of understanding of what numbers were probable.

Time Required for Task

50 minutes

Interdisciplinary Links

This problem could be nicely integrated with a social studies discussion of communication systems. The dialing system will be changed because the country is running out of numbers for telephone exchanges.

Teaching Tips

You may want to have telephone books available (I may not hand them out, but if asked for one I would be ready) to give an opportunity for more students to reach a higher level of understanding.

Suggested Materials

Exemplars

- Telephone books
- Graph paper

Possible Solutions

See the Expert solution.

Benchmark Descriptors

Novice

There is no accurate solution, little evidence of a strategy or reasoning and little explanation.

Apprentice

The student uses a strategy that is partially useful. There is some evidence of reasoning, but an incomplete explanation for finding how many numbers were not probable.

Practitioner

This student has a broad understanding of the problem and uses a strategy that finds all numbers if 10 digits are allowed for each slot. S/he uses effective reasoning in subtracting out the improbable numbers. His/her explanation is clear.

Expert

This student shows a deep understanding of the problem and is solving a realistic interpretation of the problem efficiently. S/he is explaining and subtracting out the impossible combinations as s/he sets up the problem.